

## 5

## Linear Equations in Two Variables

## Problem set 5

(1) Choose the correct alternative answers for the following questions.

(i) If  $3x + 5y = 9$  and  $5x + 3y = 7$  then What is the value of  $x + y$  ?

- (A) 2                      (B) 16                      (C) 9                      (D) 7

Soln:-

$$3x + 5y = 9$$

+

$$5x + 3y = 7$$

---


$$8x + 8y = 16$$

$$\therefore \boxed{x + y = 2}$$

Option - (A)

(ii) 'When 5 is subtracted from length and breadth of the rectangle, the perimeter becomes 26.' What is the mathematical form of the statement ?

- (A)  $x - y = 8$       (B)  $x + y = 8$       (C)  $x + y = 23$       (D)  $2x + y = 21$

Soln:-

$$\text{Length} = x - 5$$

$$\& \text{ Breadth} = y - 5$$

$$\therefore \text{Perimeter} = 2 (\text{Length} + \text{Breadth})$$

$$26 = 2 (x - 5 + y - 5)$$

$$13 = x + y - 10$$

$$x + y = 13 + 10$$

$$x + y = 23$$

Option (c)

(iii) Ajay is younger than Vijay by 5 years. Sum of their ages is 25 years. What is Ajay's age ?

- (A) 20      (B) 15      (C) 10      (D) 5

Sol<sup>n</sup>:- Let, Ajay's age =  $x$  years.

Vijay's age =  $x + 5$  years

And, sum of their ages is 25 years.

$$x + x + 5 = 25$$

$$2x = 25 - 5$$

$$2x = 20$$

$$x = 20 / 2$$

$\therefore$

$$x = 10$$

Option (c)

(2) Solve the following simultaneous equations.

(i)  $2x + y = 5$  ;  $3x - y = 5$

(ii)  $x - 2y = -1$  ;  $2x - y = 7$

(iii)  $x + y = 11$  ;  $2x - 3y = 7$

(iv)  $2x + y = -2$  ;  $3x - y = 7$

(v)  $2x - y = 5$  ;  $3x + 2y = 11$

(vi)  $x - 2y = -2$  ;  $x + 2y = 10$

Sol<sup>n</sup>:-

i)  $2x + y = 5$  ;  $3x - y = 5$

$$2x + y = 5 \quad \text{---} \quad \textcircled{\text{I}}$$

$$3x - y = 5 \quad \text{---} \quad \textcircled{\text{II}}$$

Add eq<sup>s</sup>  $\textcircled{\text{I}}$  and eq<sup>s</sup>  $\textcircled{\text{II}}$  ,

$$\begin{array}{r} 2x + \cancel{y} = 5 \\ + \\ 3x - \cancel{y} = 5 \\ \hline 5x = 10 \end{array}$$

$$\therefore x = \frac{10}{5}$$

$$\therefore \boxed{x = 2}$$

Put  $x = 2$  in eq<sup>s</sup>  $\textcircled{\text{I}}$  ,

$$2x + y = 5$$

$$(2 \times 2) + y = 5$$

$$4 + y = 5$$

$$\therefore y = 5 - 4$$

$$\therefore \boxed{y = 1}$$

$$\text{Solution} = (x, y) = (2, 1)$$

ii)  $x - 2y = -1$  ;  $2x - y = 7$

$$x - 2y = -1 \quad \text{---} \quad \textcircled{\text{I}}$$

$$2x - y = 7 \quad \text{---} \quad \textcircled{\text{II}}$$

Multiply eq<sup>n</sup>  $\textcircled{\text{II}}$  by 2,

$$4x - 2y = 14 \quad \text{---} \quad \textcircled{\text{III}}$$

Subtract eq<sup>n</sup>  $\textcircled{\text{I}}$  from eq<sup>n</sup>  $\textcircled{\text{III}}$ ,

$$\begin{array}{r} 4x - 2y = 14 \\ - \quad x - 2y = -1 \\ \hline \quad - \quad + \quad + \\ 3x \quad = 15 \end{array}$$

$$\therefore x = \frac{15}{3}$$

$$\therefore \boxed{x = 5}$$

Put  $x = 5$  in eq<sup>n</sup>  $\textcircled{\text{I}}$ ,

$$x - 2y = -1$$

$$5 - 2y = -1$$

$$2y = 5 + 1$$

$$2y = 6$$



$$y = \frac{6}{2}$$

$\therefore$

$$y = 3$$

$$\text{Solution} = (x, y) = (5, 3)$$

$$\text{iii) } x + y = 11 \quad ; \quad 2x - 3y = 7$$

$$x + y = 11 \quad \text{---} \quad \textcircled{\text{I}}$$

$$2x - 3y = 7 \quad \text{---} \quad \textcircled{\text{II}}$$

Multiply eq<sup>n</sup>  $\textcircled{\text{I}}$  by 3,

$$3x + 3y = 33 \quad \text{---} \quad \textcircled{\text{III}}$$

Add eq<sup>n</sup>  $\textcircled{\text{II}}$  and eq<sup>n</sup>  $\textcircled{\text{III}}$ ,

$$2x - \cancel{3y} = 7$$

$$+ \quad 3x + \cancel{3y} = 33$$

---

$$5x = 40$$

$$\therefore x = \frac{40}{5}$$

$\therefore$

$$x = 8$$

Put  $x = 8$  in eq<sup>n</sup>  $\textcircled{\text{I}}$ ,

$$x + y = 11$$

$$\therefore 8 + y = 11$$

$$\therefore y = 11 - 8$$

$$\therefore y = 3$$

$$\therefore \text{Solution} = (x, y) = (8, 3)$$

$$\text{iv) } 2x + y = -2 \quad ; \quad 3x - y = 7$$

$$2x + y = -2 \quad \text{--- (I)}$$

$$3x - y = 7 \quad \text{--- (II)}$$

Add eq<sup>n</sup> (I) and eq<sup>n</sup> (II),

$$\begin{array}{r} 2x + \cancel{y} = -2 \\ + \quad 3x - \cancel{y} = 7 \\ \hline 5x = 5 \end{array}$$

$$\therefore x = \frac{5}{5}$$

$$\therefore x = 1$$

Put  $x = 1$  in eq<sup>n</sup> (I),

$$2x + y = -2$$

$$(2 \times 1) + y = -2$$

$$2 + y = -2$$

$$y = -2 - 2$$

$$\therefore y = -4$$

$$\therefore \text{Solution} = (x, y) = (1, -4)$$

$$v) \quad 2x - y = 5 \quad ; \quad 3x + 2y = 11$$

$$2x - y = 5 \quad \text{---} \quad \textcircled{\text{I}}$$

$$3x + 2y = 11 \quad \text{---} \quad \textcircled{\text{II}}$$

Multiply eq<sup>n</sup>  $\textcircled{\text{I}}$  by 2,

$$4x - 2y = 10 \quad \text{---} \quad \textcircled{\text{III}}$$

Add eq<sup>n</sup>  $\textcircled{\text{II}}$  and eq<sup>n</sup>  $\textcircled{\text{III}}$ ,

$$3x + \cancel{2y} = 11$$

$$+ \quad 4x - \cancel{2y} = 10$$

---

$$7x = 21$$

$$\therefore x = \frac{21}{7}$$

$\therefore$

$$x = 3$$

Put  $x = 3$  in eqn (I),

$$2x - y = 5$$

$$\therefore (2 \times 3) - y = 5$$

$$\therefore 6 - 5 = y$$

$$\therefore y = 1$$

$$\therefore \text{Solution} = (x, y) = (3, 1)$$

$$\text{vi) } x - 2y = -2 ; \quad x + 2y = 10$$

$$x - 2y = -2 \quad \text{--- (I)}$$

$$x + 2y = 10 \quad \text{--- (II)}$$

Add eqn (I) and eqn (II)

$$x - \cancel{2y} = -2$$

$$+ \quad x + \cancel{2y} = 10$$

---

$$2x = 8$$

$$\therefore x = \frac{8}{2}$$

$$\therefore x = 4$$

Put  $x = 4$  in eq<sup>n</sup> ①,

$$x - 2y = -2$$

$$\therefore 4 - 2y = -2$$

$$\therefore 2y = 4 + 2$$

$$\therefore 2y = 6$$

$$\therefore y = \frac{6}{2}$$

$$\therefore y = 3$$

$$\therefore \text{Solution} = (x, y) = (4, 3)$$

(3) By equating coefficients of variables, solve the following equations.

(i)  $3x - 4y = 7$ ;  $5x + 2y = 3$

(ii)  $5x + 7y = 17$ ;  $3x - 2y = 4$

(iii)  $x - 2y = -10$ ;  $3x - 5y = -12$

(iv)  $4x + y = 34$ ;  $x + 4y = 16$

Sol<sup>n</sup>:-

i)  $3x - 4y = 7$  ;  $5x + 2y = 3$

$$3x - 4y = 7 \quad \text{---} \quad \text{①}$$

$$5x + 2y = 3 \quad \text{---} \quad \text{②}$$

Multiply eq<sup>n</sup> ② by 2,

$$10x + 4y = 6 \quad \text{--- (III)}$$

Add eq<sup>n</sup> (I) and eq<sup>n</sup> (III),

$$\begin{array}{r} 3x - 4y = 7 \\ + \\ 10x + 4y = 6 \\ \hline 13x = 13 \end{array}$$

$$\therefore x = \frac{13}{13}$$

$$\therefore \boxed{x = 1}$$

Put  $x = 1$  in eq<sup>n</sup> (I),

$$3x - 4y = 7$$

$$(3 \times 1) - 4y = 7$$

$$4y = 3 - 7$$

$$\therefore 4y = -4$$

$$\therefore y = \frac{-4}{4}$$

$$\therefore \boxed{y = -1}$$

$$\therefore \text{Solution} = (x, y) = (1, -1)$$

$$\text{ii) } 5x + 7y = 17 \quad ; \quad 3x - 2y = 4$$

$$5x + 7y = 17 \quad \text{---} \quad \textcircled{\text{I}}$$

$$3x - 2y = 4 \quad \text{---} \quad \textcircled{\text{II}}$$

Multiply eq<sup>n</sup>  $\textcircled{\text{I}}$  by 2 and eq<sup>n</sup>  $\textcircled{\text{II}}$  by 7,

$$10x + 14y = 34 \quad \text{---} \quad \textcircled{\text{III}}$$

$$21x - 14y = 28 \quad \text{---} \quad \textcircled{\text{IV}}$$

Add eq<sup>n</sup>  $\textcircled{\text{III}}$  and eq<sup>n</sup>  $\textcircled{\text{IV}}$ ,

$$\begin{array}{r} 10x + \cancel{14y} = 34 \\ + \quad 21x - \cancel{14y} = 28 \\ \hline 31x \qquad \qquad = 62 \end{array}$$

$$\therefore x = \frac{62}{31}$$

$$\therefore \boxed{x = 2}$$

Put  $x = 2$  in eq<sup>n</sup>  $\textcircled{\text{I}}$ .

$$5x + 7y = 17$$

$$(5 \times 2) + 7y = 17$$

$$10 + 7y = 17$$

$$7y = 17 - 10$$

$$7y = 7$$

$$y = \frac{7}{7}$$

$$y = 1$$

$$\therefore \text{Solution} = (x, y) = (2, 1)$$

$$\text{iii) } x - 2y = -10 \quad ; \quad 3x - 5y = -12$$

$$x - 2y = -10 \quad \text{---} \quad \textcircled{\text{I}}$$

$$3x - 5y = -12 \quad \text{---} \quad \textcircled{\text{II}}$$

Multiply eq?  $\textcircled{\text{I}}$  by 3,

$$3x - 6y = -30 \quad \text{---} \quad \textcircled{\text{III}}$$

Subtract eq?  $\textcircled{\text{II}}$  from eq?  $\textcircled{\text{III}}$ ,

$$\begin{array}{r} \cancel{3x} - 6y = -30 \\ - \quad \cancel{3x} - 5y = -12 \\ \hline \quad \quad +y = +18 \end{array}$$

$\therefore$

$$y = 18$$

Put  $y = 18$  in eq?  $\textcircled{\text{I}}$ ,



$$x - 2y = -10$$

$$x - (2 \times 18) = -10$$

$$x - 36 = -10$$

$$x = -10 + 36$$

$\therefore$

$$x = 26$$

$$\therefore \text{Solution} = (x, y) = (26, 18)$$

$$\text{iv) } 4x + y = 34 \quad ; \quad x + 4y = 16$$

$$4x + y = 34 \quad \text{--- (I)}$$

$$x + 4y = 16 \quad \text{--- (II)}$$

Multiply eq? (II) by 4 ,

$$4x + 16y = 64 \quad \text{--- (III)}$$

Subtract eq? (I) from eq? (III) ,

$$\begin{array}{r} \cancel{4x} + 16y = 64 \\ - \quad \cancel{4x} + y = 34 \\ \hline 15y = 30 \end{array}$$

$$y = \frac{30}{15}$$

$\therefore$

$$y = 2$$

Put  $y = 2$  in eq? (I) ,

$$4x + y = 34$$

$$4x + 2 = 34$$

$$4x = 34 - 2$$

$$4x = 32$$

$$x = \frac{32}{4}$$

$$x = 8$$

$\therefore$  Solution =  $(x, y) = (8, 2)$

(4) Solve the following simultaneous equations.

(i)  $\frac{x}{3} + \frac{y}{4} = 4$  ;  $\frac{x}{2} - \frac{y}{4} = 1$

(ii)  $\frac{x}{3} + 5y = 13$  ;  $2x + \frac{y}{2} = 19$

(iii)  $\frac{2}{x} + \frac{3}{y} = 13$  ;  $\frac{5}{x} - \frac{4}{y} = -2$

Soln:-

i)  $\frac{x}{3} + \frac{y}{4} = 4$  ;  $\frac{x}{2} - \frac{y}{4} = 1$

$$\frac{x}{3} + \frac{y}{4} = 4$$

$$\overset{4}{\cancel{12}} \times \frac{x}{\cancel{3}_1} + \overset{3}{\cancel{12}} \times \frac{y}{\cancel{4}_1} = 12 \times 4$$

$$4x + 3y = 48 \quad \text{--- (I)}$$

$$\frac{x}{2} - \frac{y}{4} = 1$$

$$\overset{4}{\cancel{8}} \times \frac{x}{\cancel{2}_1} - \overset{2}{\cancel{8}} \times \frac{y}{\cancel{4}_1} = 8$$

$$4x - 2y = 8 \quad \text{--- (II)}$$

Subtract eq<sup>n</sup> (II) from eq<sup>n</sup> (I),

$$\cancel{4x} + 3y = 48$$

$$- \cancel{4x} - 2y = 8$$

$$\begin{array}{r} - \quad + \quad - \\ \hline 5y = 40 \end{array}$$

$$y = \frac{40}{5}$$

∴

$$y = 8$$

Put  $y = 8$  in eq<sup>n</sup> (II),

$$4x - 2y = 8$$

$$4x - (2 \times 8) = 8$$

$$4x - 16 = 8$$

$$4x = 8 + 16$$

$$4x = 24$$

$$\therefore x = \frac{24}{4}$$

$$\therefore \boxed{x = 6}$$

$$\therefore \text{Solution} = (x, y) = (6, 8)$$

$$\text{ii)} \quad \frac{x}{3} + 5y = 13 \quad ; \quad 2x + \frac{y}{2} = 19$$

$$\frac{x}{3} + 5y = 13$$

$$\cancel{3} \times \frac{x}{\cancel{3}} + 3 \times 5y = 3 \times 13$$

$$x + 15y = 39 \quad \text{--- (I)}$$

$$2x + \frac{y}{2} = 19$$

$$30 \times 2x + \cancel{30}^{\text{15}} \times \frac{y}{\cancel{2}} = 30 \times 19$$

$$60x + 15y = 570 \quad \text{--- (II)}$$

Subtract eq<sup>n</sup> (I) from eq<sup>n</sup> (II),

$$60x + \cancel{15y} = 570$$

$$- \quad x + \cancel{15y} = 39$$

$$59x = 531$$

$$\therefore x = \frac{531}{59}$$

$$\therefore \boxed{x = 9}$$

Put  $x=9$  in eq? (I),

$$x + 15y = 39$$

$$9 + 15y = 39$$

$$15y = 39 - 9$$

$$15y = 30$$

$$\therefore y = \frac{30}{15}$$

$$\therefore \boxed{y = 2}$$

$$\therefore \text{Solution} = (x, y) = (9, 2)$$

$$\text{iii)} \quad \frac{2}{x} + \frac{3}{y} = 13 ; \quad \frac{5}{x} - \frac{4}{y} = -2$$

$$\text{Let, } \frac{1}{x} = m \quad \& \quad \frac{1}{y} = n$$

$$2m + 3n = 13 \quad \text{--- (I)}$$

$$5m - 4n = -2 \quad \text{--- (I)}$$

Multiply eq? (I) by 4 and eq? (II) by 3,

$$8m + 12n = 52 \quad \text{--- (III)}$$

$$15m - 12n = -6 \quad \text{--- (IV)}$$

Add eq? (III) and eq? (IV),

$$8m + \cancel{12n} = 52$$

$$+ \quad 15m - \cancel{12n} = -6$$

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$$23m = 46$$

$$\therefore m = \frac{46}{23}$$

$$\therefore m = 2$$

Put  $m = 2$  in eq? (I),

$$2m + 3n = 13$$

$$(2 \times 2) + 3n = 13$$

$$4 + 3n = 13$$

$$\therefore 3n = 13 - 4$$

$$\therefore 3n = 9$$

$$\therefore n = \frac{9}{3}$$

$$\therefore \boxed{n = 3}$$

Now,

$$m = 2 \quad \& \quad n = 3$$

$$\therefore \frac{1}{x} = 2 \quad \& \quad \frac{1}{y} = 3$$

$$\therefore \boxed{x = \frac{1}{2}} \quad \& \quad \boxed{y = \frac{1}{3}}$$

$$\therefore \text{Solution} = (x, y) = \left(\frac{1}{2}, \frac{1}{3}\right)$$

(5\*) A two digit number is 3 more than 4 times the sum of its digits. If 18 is added to this number, the sum is equal to the number obtained by interchanging the digits. Find the number.

Soln:- Let, the digit at the unit place

be 'x' and the digit at the tens place

be 'y'.

$\therefore$  The two digit number is,

$$10y + x$$

Now, the two digit number is 3 more

than 4 times the sum of its digits.

$$\therefore 10y + x = 4(x + y) + 3$$

$$\therefore 10y + x = 4x + 4y + 3$$

$$\therefore 10y + x - 4x - 4y = 3$$

$$\therefore -3x + 6y = 3$$

$$\therefore -x + 2y = 1 \text{ ——— } \textcircled{\text{I}}$$

If 18 is added to this number, the sum is equal to the number obtained by interchanging the digits.

$$10y + x + 18 = 10x + y$$

$$\therefore 10y + x - 10x - y = -18$$

$$\therefore -9x + 9y = -18$$

$$\therefore -x + y = -2 \text{ ——— } \textcircled{\text{II}}$$

Subtract eq<sup>n</sup>  $\textcircled{\text{I}}$  from eq<sup>n</sup>  $\textcircled{\text{II}}$ ,

$$- \cancel{x} + y = -2$$

$$- \quad - \cancel{x} + 2y = 1$$

$$+ \quad - \quad -$$

---


$$-y = -3$$

$$\therefore \boxed{y = 3}$$



Put  $y=3$  in eqn (I),

$$-x + 2y = 1$$

$$-x + (2 \times 3) = 1$$

$$-x + 6 = 1$$

$$-x = 1 - 6$$

$$-x = -5$$

$$\therefore \boxed{x = 5}$$

$\therefore$  The two digit number is,

$$= 10y + x$$

$$= (10 \times 3) + 5$$

$$= 30 + 5$$

$$= 35$$

- (6) The total cost of 8 books and 5 pens is 420 rupees and the total cost of 5 books and 8 pens is 321 rupees. Find the cost of 1 book and 2 pens.

Soln:-

Let, the cost of 1 book and 1 pen

be  $x$  and  $y$  rupees respectively.

Now, the total cost of 8 books and 5

pens is 420 rupees.

$$8x + 5y = 420 \quad \text{--- (I)}$$

Also, the total cost of 5 books and 8 pens is 321 rupees.

$$5x + 8y = 321 \quad \text{--- (II)}$$

Multiply eq<sup>n</sup> (I) by 8 and eq<sup>n</sup> (II) by 5,

$$64x + 40y = 3360 \quad \text{--- (III)}$$

$$25x + 40y = 1605 \quad \text{--- (IV)}$$

Subtract eq<sup>n</sup> (III) from eq<sup>n</sup> (IV),

$$\begin{array}{r} 64x + \cancel{40y} = 3360 \\ - 25x + \cancel{40y} = 1605 \\ \hline 39x = 1755 \end{array}$$

$$\therefore x = \frac{1755}{39}$$

$$\therefore \boxed{x = 45}$$

Put  $x = 45$  in eq<sup>n</sup> (I),

$$8x + 5y = 420$$

$$\therefore (45 \times 8) + 5y = 420$$

$$\therefore 360 + 5y = 420$$

$$\therefore 5y = 420 - 360$$

$$\therefore 5y = 60$$

$$\therefore y = \frac{60}{5}$$

$$\therefore y = 12$$

$\therefore$  The cost of 1 book & 2 pens

$$= x + 2y$$

$$= 45 + 2 \times 12$$

$$= 45 + 24$$

$$= ₹ 69$$

(7\*) The ratio of incomes of two persons is 9 : 7. The ratio of their expenses is 4 : 3. Every person saves rupees 200, find the income of each.

Soln:-

Let, the income of two persons be  $x$  and  $y$  rupees respectively.

Now, the ratio of their incomes is 9:7

$$\therefore \frac{x}{y} = \frac{9}{7}$$

$$\therefore 7x = 9y$$

$$\therefore 7x - 9y = 0 \quad \text{--- (I)}$$

Also, the ratio of their expenses is 4:3  
and each person saves rupees 200.

$$\text{Income} - \text{Savings} = \text{Expenses}$$

$$\therefore \frac{x - 200}{y - 200} = \frac{4}{3}$$

$$\therefore 3(x - 200) = 4(y - 200)$$

$$\therefore 3x - 600 = 4y - 800$$

$$\therefore 3x - 4y = -800 + 600$$

$$\therefore 3x - 4y = -200 \quad \text{--- (II)}$$

Multiply eq<sup>n</sup> (I) by 3 and eq<sup>n</sup> (II) by 7,

$$21x - 27y = 0 \quad \text{--- (III)}$$

$$21x - 28y = -1400 \quad \text{--- (IV)}$$

Subtract eq<sup>n</sup> (III) from eq<sup>n</sup> (IV),

$$\begin{array}{r}
 \cancel{21}x - 28y = -1400 \\
 - \quad \cancel{21}x - 27y = 0 \\
 \hline
 -y = -1400
 \end{array}$$

$$\therefore y = 1400$$

Put  $y = 1400$  in eq<sup>n</sup> (I),

$$7x - 9y = 0$$

$$7x = 9y$$

$$7x = 9 \times 1400$$

$$\therefore x = \frac{9 \times \overset{200}{\cancel{1400}}}{\cancel{7}}$$

$$\therefore x = 1800$$

$\therefore$  The income of two persons is  
₹ 1800 & ₹ 1400 respectively.

(8\*) If the length of a rectangle is reduced by 5 units and its breadth is increased by 3 units, then the area of the rectangle is reduced by 8 square units. If length is reduced by 3 units and breadth is increased by 2 units, then the area of rectangle will increase by 67 square units. Then find the length and breadth of the rectangle.

Sol<sup>n</sup>:-

Let, the length and breadth of the

rectangle be  $x$  and  $y$  units respectively.

$\therefore$  Area of rectangle ,

$$= \text{length} \times \text{breadth}$$

$$= xy \text{ sq. units}$$

Now, if the length is reduced by 5 units and its breadth is increased by 3 units , then the area of the rectangle is reduced by 8 square units.

$$\therefore (x-5)(y+3) = xy - 8$$

$$\therefore \cancel{xy} + 3x - 5y - 15 = \cancel{xy} - 8$$

$$\therefore 3x - 5y = 15 - 8$$

$$\therefore 3x - 5y = 7 \quad \text{--- (I)}$$

Also , if the length is reduced by 3 units and its breadth is increased by 2 units , then the area of the rectangle will increase by 67 square units.

$$(x-3)(y+2) = xy + 67$$

$$\cancel{2x}y + 2x - 3y - 6 = \cancel{x}y + 67$$

$$2x - 3y = 67 + 6$$

$$\therefore 2x - 3y = 73 \quad \text{--- (II)}$$

Multiply eq<sup>n</sup> (I) by 2 and eq<sup>n</sup> (II) by 3,

$$6x - 10y = 14 \quad \text{--- (III)}$$

$$6x - 9y = 219 \quad \text{--- (IV)}$$

Subtract eq<sup>n</sup> (III) from eq<sup>n</sup> (IV),

$$\cancel{6x} - 9y = 219$$

$$\begin{array}{r} - \quad \cancel{6x} - 10y = 14 \\ - \quad \quad + \quad \quad - \\ \hline y = 205 \end{array}$$

$$\therefore \boxed{y = 205}$$

Put  $y = 205$  in eq<sup>n</sup> (I),

$$3x - 5y = 7$$

$$3x - (5 \times 205) = 7$$

$$3x - 1025 = 7$$

$$3x = 7 + 1025$$

$$\therefore 3x = 1032$$

$$\therefore x = \frac{1032}{3}$$

$$\therefore x = 344$$

$\therefore$  The length of the rectangle is 344 units and the breadth of the rectangle is 205 units.

(9\*) The distance between two places A and B on road is 70 kilometers. A car starts from A and the other from B. If they travel in the same direction, they will meet after 7 hours. If they travel towards each other they will meet after 1 hour, then find their speeds.

Soln:-

Let, the speeds of the cars be  $x$  km per hour and  $y$  km per hour respectively.

$$\text{Now, Speed} = \frac{\text{Distance}}{\text{Time}}$$

Now, if they travel in same direction then they will meet after 7 hours.

$$x - y = \frac{70}{7}$$

$$\therefore x - y = 10 \quad \text{--- (I)}$$



Also, if they travel towards each other then they will meet after 1 hour.

$$\therefore x + y = \frac{70}{1}$$

$$\therefore x + y = 70 \quad \text{--- } \textcircled{II}$$

Add eq<sup>n</sup>  $\textcircled{I}$  and eq<sup>n</sup>  $\textcircled{II}$ ,

$$\begin{array}{r} x - \cancel{y} = 10 \\ + \\ x + \cancel{y} = 70 \\ \hline 2x = 80 \end{array}$$

$$\therefore x = \frac{80}{2}$$

$$\therefore \boxed{x = 40}$$

Put  $x = 40$  in eq<sup>n</sup>  $\textcircled{I}$ ,

$$x - y = 10$$

$$\therefore 40 - y = 10$$

$$\therefore y = 40 - 10$$

$$\therefore \boxed{y = 30}$$

$\therefore$  The speeds of the cars are 40 km/Hr and 30 km/Hr respectively.

(10\*) The sum of a two digit number and the number obtained by interchanging its digits is 99. Find the number.

Soln:-

Let, the digit at the unit place be 'x' and the digit at the tens place be 'y'.

$\therefore$  The two digit number is,

$$= 10y + x$$

Now, the number obtained by interchanging the digits is,

$$= 10x + y$$

Now, their sum is 99.

$$10y + x + 10x + y = 99$$

$$11x + 11y = 99$$

$$\therefore x + y = 9 \text{ — (I)}$$

The information given here is insufficient.

If  $x = 1$  , then

$$1 + y = 9$$

$$y = 9 - 1$$

$$y = 8$$

Similarly , when  $x = 2$  then  $y = 7$

when  $x = 3$  then  $y = 6$

when  $x = 4$  then  $y = 5$

when  $x = 5$  then  $y = 4$

when  $x = 6$  then  $y = 3$

when  $x = 7$  then  $y = 2$

when  $x = 8$  then  $y = 1$

$\therefore$  The number could be ,

81 , 72 , 63 , 54 , 45 , 36 , 27 , 18 .